

7. RISK ANALYSIS IN CAPITAL BUDGETING**ASSIGNMENT SOLUTIONS****PROBLEM NO:1**

Estimation of Expected Net Cash Flows:

| Assumption (1) | Cash Flows (Rs.) (2) | Probability (3) | Expected cash flow(2x3) (Rs.) |
|-------------------------------|----------------------|-----------------|-------------------------------|
| Best guess | 9,00,000 | 0.3 | 9,00,000 × 0.3 = 2,70,000 |
| High guess | 5,00,000 | 0.4 | 5,00,000 × 0.4 = 2,00,000 |
| Low guess | 2,00,000 | 0.3 | 2,00,000 × 0.3 = 60,000 |
| Expected Net cash flow (ENCF) | | | = 5,30,000 |

PROBLEM NO: 2

Expected Investment: (Rs. 70,00,000 × 0.20) + (Rs. 80,00,000 × 0.40) + (Rs. 90,00,000 × 0.40)
 = Rs.14,00,000 + Rs.32,00,000 + Rs.36,00,000 = Rs.82,00,000

PROBLEM NO: 3

| No. of units (1) | Selling Price (2) | Probability (3) | Expected Selling Price (4) | Variable Cost (5) | Probability (6) | Expected Variable Cost (7) | Expected Cash Flow (Rs.) {1 x (4 - 7)} |
|----------------------------------|-------------------|-----------------|----------------------------|-------------------|-----------------|----------------------------|--|
| 40,000 | 10 | 0.3 | 3 | 5 | 0.3 | 1 | 80,000 |
| 40,000 | 20 | 0.4 | 8 | 10 | 0.4 | 3.5 | 1,80,000 |
| 40,000 | 30 | 0.3 | 9 | 15 | 0.40 | 6 | 1,20,000 |
| Expected Cash Inflows | | | | | | | 3,80,000 |
| Less: Fixed Cost (P.a) | | | | | | | (1,20,000) |
| Less: Annual Depreciation | | | | | | | (50,000) |
| EBIT/ EBT | | | | | | | 2,10,000 |
| Less: Taxes @ 50% | | | | | | | (1,05,000) |
| EAT | | | | | | | 1,05,000 |
| Add: Depreciation | | | | | | | 50,000 |
| Expected CFAT | | | | | | | 1,65,000 |

Note: Students are advised to rectify the hint answer given in our material

PROBLEM NO: 4

| Possible event | Project A | | | Project B | | |
|----------------|----------------------|-------------|----------------|----------------------|-------------|----------------------|
| | Net cash Flows (Rs.) | probability | Expected value | Net Cash Flows (Rs.) | probability | Expected Value (Rs.) |
| A | 5,000 | 0.20 | 1,000 | 15,000 | 0.10 | 1,500 |
| B | 8,000 | 0.10 | 800 | 19,000 | 0.15 | 2,850 |
| C | 10,000 | 0.50 | 5,000 | 16,000 | 0.50 | 8,000 |
| D | 13,000 | 0.10 | 1,300 | 12,000 | 0.15 | 1,800 |
| E | 15,000 | 0.10 | 1,500 | 10,000 | 0.10 | 1,000 |
| ENCF | | | 9,600 | | | 15,150 |

The Net Present Value of Project A is (0.893 × Rs. 9,600 - Rs. 9,000) = Rs.427

The Net Present Value of Project B is (0.893 × Rs. 15,150 - Rs. 10,000) = Rs. 4,529

Project B is preferable

Note: Students are advised to rectify the hint answer given in our material.

PROBLEM NO: 5

| Year 1 | | | Year 2 | | | Year 3 | | |
|-----------------|-------------|----------------------|-----------------|-------------|----------------------|-----------------|-------------|----------------------|
| Cash Flow (Rs.) | Probability | Expected Value (Rs.) | Cash Flow (Rs.) | Probability | Expected Value (Rs.) | Cash Flow (Rs.) | Probability | Expected Value (Rs.) |
| 3,000 | 0.1 | 300 | 4,000 | 0.3 | 1,200 | 5,000 | 0.4 | 2,000 |
| 6,000 | 0.2 | 1,200 | 6,000 | 0.4 | 2,400 | 10,000 | 0.2 | 2,000 |
| 9,000 | 0.3 | 2,700 | 9,000 | 0.2 | 1,800 | 13,000 | 0.1 | 1,300 |
| 12,000 | 0.4 | 4,800 | 12,000 | 0.1 | 1,200 | 16,000 | 0.3 | 4,800 |
| ENCF | | 9,000 | | | 6,600 | | | 10,100 |

The present value of the expected value of cash flow at 10% discount rate has been determined as follows:

$$\text{Present Value of Cash Flow} = \frac{\text{ENCF}_1}{(1+k)^1} + \frac{\text{ENCF}_2}{(1+k)^2} + \frac{\text{ENCF}_3}{(1+k)^3} = \frac{9,000}{(1.12)^1} + \frac{6,600}{(1.12)^2} + \frac{10,100}{(1.12)^3}$$

$$= 9,000 \times 0.893 + 6,600 \times 0.797 + 10,100 \times 0.712 = \text{Rs. } 20,488$$

Expected Net Present Value = Present Value of Cash Flow - Initial Investment

$$= \text{Rs. } 20,488 - \text{Rs. } 15,000 = \text{Rs. } 5,488$$

PROBLEM NO: 6

Estimation of Variance, Standard Deviation(s) & Co-efficient of variation of each of the projects:

| Possible Event | Project M | | | | | Project N | | | | |
|----------------|---------------------|-------------|--------------------|--------|-------------|-----------------|-------------|--------------------|--------|-----------|
| | Cash Flow (Rs.) (x) | Probability | Expected Cash Flow | d_M | $P d_M^2$ | Cash Flow (Rs.) | Probability | Expected Cash Flow | d_N | $P d_N^2$ |
| P | 12,000 | 0.10 | 1,200 | -6,000 | 36,00,000 | 24,000 | 0.30 | 4,200 | -3,400 | 34,68,000 |
| Q | 15,000 | 0.30 | 4,500 | -3,000 | 27,00,000 | 16,000 | 0.20 | 3,200 | -1,400 | 3,92,000 |
| R | 18,000 | 0.20 | 3,600 | 0 | 0 | 18,000 | 0.20 | 3,600 | 600 | 72,000 |
| S | 21,000 | 0.30 | 6,300 | 3,000 | 27,00,000 | 20,000 | 0.10 | 2,000 | 2,600 | 6,76,000 |
| T | 24,000 | 0.10 | 2,400 | 6,000 | 36,00,000 | 22,000 | 0.20 | 4,400 | 4,600 | 42,32,000 |
| | | | 18,000 | | 1,26,00,000 | | | 17,400 | | 88,40,000 |

$$\text{Standard deviation for Project M} = \sqrt{1,26,00,000} = 3,549.64$$

$$\text{Standard deviation for Project N} = \sqrt{88,40,000} = 2,973.21$$

| Projects | Coefficient of variation | Risk |
|----------|------------------------------------|------|
| M | $\frac{3,549.64}{18,000} = 0.1972$ | More |
| N | $\frac{2,973.21}{17,400} = 0.1708$ | Less |

Conclusion: Project N should be selected.

Note: Students are advised to rectify the hint answer given in our material

PROBLEM NO: 7

The expected Value of cash flows of project X and Y may be calculated as follows:

$$\text{Project X} = 2,000 (0.3) + 4,000 (0.4) + 6,000 (0.3) = 4,000$$

$$\text{Project Y} = 1,000 (0.1) + 3,000 (0.1) + 5,000 (0.4) + 7,000 (0.3) + 9,000 (0.1) = 5,400$$

Now the standard deviations of two projects may be calculated as follows:

| Project X | | | | Project Y | | | |
|-----------|-------|-------|------------------------------|-----------|-------|-------|------------------------------|
| CF(Rs.) | EVCF | Prob. | $P(\text{CF}-\text{EVCF})^2$ | CF(Rs.) | EVCF | Prob. | $P(\text{CF}-\text{EVCF})^2$ |
| 2,000 | 4,000 | 0.3 | 12,00,000 | 1,000 | 5,400 | 0.1 | 19,36,000 |
| 4,000 | 4,000 | 0.4 | 0 | 3,000 | 5,400 | 0.1 | 5,76,000 |

| | | | | | | | |
|-------|-------|-----|-----------|-------|-------|-----|-----------|
| 6,000 | 4,000 | 0.3 | 12,00,000 | 5,000 | 5,400 | 0.4 | 64,000 |
| | | | | 7,000 | 5,400 | 0.3 | 7,68,000 |
| | | | | 9,000 | 5,400 | 0.1 | 12,96,000 |
| | | | 24,00,000 | | | | 46,40,000 |

Now, the standard deviation of Project X is square root of 24,00,000 i.e., 1,549 and the standard deviation of project Y is the Square root of 46,40,000 i.e., 2,154. Between these two projects X and Y, the project Y is having higher expected value of cash flows i.e., 5,400. However, it also has a higher standard deviation of 2,154 signifying that the cash flows of project X. Had the expected values of cash flows of both the projects were same, the firm must have a preference for project X. Moreover, the decision in favor of Project X would hold good as both the projects are of equal size and require equal amount of cash outlays. As the expected value of cash flows from these two projects are not same, therefore, the standard deviation as measure of risk will not help much. The reason being that the standard deviation is an absolute measure of risk and represents the risk in terms of the measuring unit i.e. Rupee amount. To resolve such dilemma, another measure known as the coefficient of variation may be used.

Coefficient of Variation: A Relative measure of Risk: Coefficient of Variation (CV) is a relative measure of dispersion and can be applied in capital budgeting decision process to measure the risk of a project particularly in case when the alternative projects are of different sizes. The CV is defined as the standard deviation of the probability distribution divided by its expected value.

PROBLEM NO: 8

SOUTH PROJECT:

i) Computation of Expected NPV & Standard Deviation

| NPV(X) | Probability | Expected NPV (X) | $D_x (X-X\bar{X})$ | D_x^2 | PD_x^2 |
|--------|-------------|------------------|--------------------|---------|----------------------|
| 3 | 0.05 | 0.15 | -4.8 | 23.04 | 1.152 |
| 5 | 0.30 | 1.50 | -2.8 | 7.84 | 2.352 |
| 6 | 0.30 | 1.80 | -1.8 | 3.24 | 0.972 |
| 12 | 0.30 | 3.60 | 4.2 | 17.64 | 5.292 |
| 15 | 0.05 | 0.75 | 7.2 | 51.84 | 2.592 |
| | | X = 7.80 | | | $\sum Pdx^2 = 12.36$ |

Standard Deviation of South Project = $\sqrt{\sum Pdx^2} = \sqrt{12.36}$

$\sigma \text{ NPV} = 3.516$

ii)

| NPV(X) | Probability | Expected NPV | $D_x (X-X\bar{X})$ | D_x^2 | PD_x^2 |
|--------|-------------|--------------|--------------------|---------|----------------------|
| 3 | 0.15 | 0.45 | -4.8 | 23.04 | 3.456 |
| 5 | 0.25 | 1.25 | -2.8 | 7.84 | 1.960 |
| 6 | 0.25 | 1.50 | -1.8 | 3.24 | 0.810 |
| 12 | 0.25 | 3.00 | 4.2 | 17.64 | 4.41 |
| 15 | 0.10 | 1.60 | 7.2 | 51.84 | 5.184 |
| | | 7.80 | | | $\sum Pdx^2 = 15.82$ |

Standard Deviation = $\sqrt{\sum Pdx^2} = \sqrt{15.82} = \sigma \text{ NPV} = 3.977$

iii) **Riskier:** Since $\sigma \text{ NPV}$ for North project is more than the $\sigma \text{ NPV}$ of the South project. North project is considered as a Riskers project.

PROBLEM NO: 9

i) On the basis of standard deviation project X be chosen because it is less risky than Project Y having higher standard deviation.

ii) $CV_x = \frac{SD}{ENPV} = \frac{40,000}{60,000} = 0.67$

$CV_y = \frac{SD}{ENPV} = \frac{1,35,000}{2,27,000} = 0.595$

On the basis of Co-efficient of Variation (C.V.) Project X appears to be more risky and Y should be accepted.

iii) However, the NPV method in such conflicting situation is best because the NPV methods in compatibility of the objective of wealth maximization in terms of time value. (Project Y is suggestable under this method)

PROBLEM NO: 10

a) Using risk - free rate

| Year | Cash flows (inflows) Rs.) | PV Factor at 10% | PV of Cash flows (in flows) |
|---------------------------|---------------------------|------------------|------------------------------|
| 1 | 40,000 | 0.909 | 36,360 |
| 2 | 50,000 | 0.826 | 41,300 |
| 3 | 15,000 | 0.751 | 11,265 |
| 4 | 30,000 | 0.683 | 20,490 |
| PV of Cash inflows | | | 1,09,415 |
| Less: PV of Cash outflows | | | (1,00,000) |
| NPV | | | 9,415 |

b) Using risk - adjusted discount rate

| Year | Cash flows (inflows) Rs.) | PV Factor at 10% | PV of Cash flows (in flows) |
|---------------------------|---------------------------|------------------|------------------------------|
| 1 | 40,000 | 0.833 | 33,320 |
| 2 | 50,000 | 0.694 | 34,700 |
| 3 | 15,000 | 0.579 | 8,685 |
| 4 | 30,000 | 0.482 | 14,460 |
| PV of Cash inflows | | | 91,165 |
| Less: PV of Cash outflows | | | (1,00,000) |
| NPV | | | (8,835) |

- The project would be acceptable when no allowance is made for risk. But it will not be acceptable if risk premium is added to the risk free rate. It moves from positive NPV to negative NPV.
- If the firm were to use the internal rate of return, then the project would be accepted when IRR is greater than the risk - adjusted discount rate.

PROBLEM NO: 11

Determination of cost of debt and equity:

Volume of Debt and Equity at 50:50 works out to Rs. 1100 lakhs each.

(Rs. in Lakhs)

| Debt | 1 st Slab | 2 nd Slab | 3 rd Slab | 4 th Slab |
|-------------------------|----------------------|----------------------|----------------------|----------------------|
| Volume of funds | 500 | 500 | 100 | 1100 |
| Rate | 10% | 12% | 15.72% | |
| Interest cost | 50 | 60 | 15.72 | 125.72 |
| Tax saving 30% | | | | 37.72 |
| Post-tax cost (Int-tax) | | | | 88.00 |

Determination of weighted marginal cost of capital

| Source | Cost % | Weight | Weight x Cost % |
|----------------------|--------|--------|-----------------|
| Debt | 8.00 | 0.50 | 4.00 |
| Equity | 12.00 | 0.50 | 6.00 |
| WMCC (cut-off rate) | | 1.00 | 10.00 |

Risk Adjusted rate = Cut off rate + Risk Premium = 10 + 2 = 12%

PROBLEM NO: 12

Statement showing the determination of the risk adjusted Net Present Value:

| Projects | Net cash outlays (Rs.) | Coefficient of variation | Risk adjusted discount rate | Annual Cash inflow (Rs.) | PV factor 1-5 years | Discounted cash inflow (Rs.) | Net present value (Rs.) |
|----------|------------------------|--------------------------|-----------------------------|--------------------------|---------------------|------------------------------|-------------------------|
| (i) | (ii) | (iii) | (iv) | (v) | (vi) | (vii) = (v) × (vi) | (viii) = (vii) - (ii) |
| X | 4,00,000 | 1.6 | 18% | 2,00,000 | 3.127 | 6,25,400 | 2,25,400 |
| Y | 1,80,000 | 2.0 | 22% | 80,000 | 2.864 | 2,29,120 | 49,120 |
| Z | 2,50,000 | 1.2 | 16% | 1,25,000 | 3.274 | 4,09,250 | 1,59,250 |

PROBLEM NO: 13

Determination of NPV:

| Year | Expected CFAT | Certainty equivalent (CE) | Adjusted CFAT (CFAT X CE) | PV factor (at 0.06) | Total PV |
|------------|----------------|---------------------------|---------------------------|---------------------|-----------------|
| 0 | (Rs. 2,00,000) | 1.0 | Rs.(2,00,000) | 1.000 | (Rs.2,00,000) |
| 1 | Rs. 1,60,000 | 0.8 | Rs.1,28,000 | 0.943 | Rs.1,20,704 |
| 2 | Rs. 1,40,000 | 0.7 | Rs.98,000 | 0.890 | Rs.87,220 |
| 3 | Rs. 1,30,000 | 0.6 | Rs.78,000 | 0.840 | Rs.65,520 |
| 4 | Rs. 1,20,000 | 0.4 | Rs.48,000 | 0.792 | Rs.38,016 |
| 5 | Rs. 80,000 | 0.3 | Rs.24,000 | 0.747 | Rs.17,928 |
| NPV | | | | | 1,29,388 |

Since NPV is positive the project should be accepted.

PROBLEM NO: 14

NPV = 10,00,000 (0.90) / (1.05) + 15,00,000 (0.85) / (1.05)² + 20,00,000 (0.82) / (1.05)³ + 5,00,000 (0.78) / (1.05)⁴ - 45,00,000 = Rs.5,34,570

PROBLEM NO: 15**Part I:****Step 1: Ascertain the discount rate.**

When CE approach is adopted, risk-free rate (i.e., 8% in this case) is relevant.

Step 2: Compute NPV of the project X

| Year | Cash flow (Rs.) | Certainty factor | Certain cash flow (Rs.) | DF @ 8% | PV of cash flows (Rs.) |
|--------------------|-----------------|------------------|-------------------------|---------|------------------------|
| 0 | (3,40,000) | 1.0 | (3,40,000) | 1.000 | (3,40,000) |
| 1 | 1,80,000 | 0.8 | 1,44,000 | 0.926 | 1,33,344 |
| 2 | 2,00,000 | 0.7 | 1,40,000 | 0.857 | 1,19,980 |
| 3 | 2,00,000 | 0.5 | 1,00,000 | 0.794 | 79,400 |
| NPV (7,276) | | | | | |

Statement showing NPV of Project Y

| Year | Cash flow (Rs.) | Certainty factor | Certain cash flow (Rs.) | DF @ 8% | PV of cash flows (Rs.) |
|---------------------|-----------------|------------------|-------------------------|---------|------------------------|
| 0 | (3,30,000) | 1.0 | (3,30,000) | 1.000 | (3,30,000) |
| 1 | 1,80,000 | 0.9 | 1,62,000 | 0.926 | 1,50,012 |
| 2 | 1,80,000 | 0.8 | 1,44,000 | 0.857 | 1,23,408 |
| 3 | 2,00,000 | 0.7 | 1,40,000 | 0.794 | 1,11,160 |
| NPV = 54,580 | | | | | |

Step 3: Decision: Since the NPV of project X is negative it should be rejected. Since the NPV of project Y is positive, it should be accepted.

PART II: Project for which RADR will be applied

Since the CE coefficient is lower in project X, it is deemed to be riskier than Project Y. Project X should, therefore, be evaluated by using RADR of 10%.

PROBLEM NO: 16

NPV = -1,25,000 + [(100 - 30) 2,000 - 1,00,000] x 3.791 = Rs. 26,640

Sensitivity to changes to

| | | |
|----|---|-------------------------|
| 1. | Selling price | |
| | 125,000 = [(P - 30) 2,000 - 100,000] X 3.791 | Alternatively |
| | 32,973 = 2,000 P - 60,000 - 100,000 | <u>Rs. 26,640</u> |
| | P = 96.49 | 2,000 x Rs. 100 x 3.791 |
| | i.e. fall of 3.51% $\left[\frac{96.49 - 100}{100} \right]$ before NPV is zero. | |

| | | |
|----|---|--|
| 2. | Variable costs | |
| | $1,25,000 = [(100 - v) 2,000 - 1,00,000] \times 3.791$ | Alternatively |
| | $32,973 = 2,00,000 - 2,000V - 1,00,000$ | Rs. 26,640 |
| | $V = 33.51$ | $2,000 \times \text{Rs. } 30 \times 3.791$ |
| | i.e. increase of 11.71% $\frac{33.51 - 30}{30}$ before NPV is zero. | |
| 3. | Volume | |
| | $1,25,000 = [(100 - 30) q - 1,00,000] \times 3.791$ | Alternatively |
| | $32,973 = 70q - 100,000$ | Rs. 26,640 |
| | $q = 1,900$ | $2,000 \times \text{Rs. } (100 - 30) \times 3.791$ |
| | in fall of 5.0% $\frac{1,900 - 2,000}{2,000}$ before NPV is zero. | |
| 4. | Initial cost | Alternatively |
| | Rs. $(1,25,000 + 26,640) = \text{Rs. } 151,640$ | Rs. 26,640 |
| | i.e. increase of 21.31% $\frac{151,640 - 1,25,000}{1,25,000}$ before NPV is zero. | Rs. 1,25,000 |
| 5. | Fixed costs | Alternatively |
| | $125,000 = [(\text{Rs. } 100 - \text{Rs. } 30) 2,000 - F] \times 3.791$ | Rs. 26,640 |
| | $32,973 = 1,40,000 - F$ | Rs. $1,00,000 \times 3.791$ |
| | $F = 1,07,027$ | |
| | i.e. an increase of 7.03% $\frac{1,07,027 - 1,00,000}{1,00,000}$ before NPV is zero | |
| 6. | Life | |
| | Rs. $1,25,000 = \text{Rs. } 40,000 \times \text{AF}_n @ 10\%$ | |
| | $3.125 = \text{AF}_n @ 10\%$ | |
| | AF for 4 years at 10% is 3.17 | |
| | i.e. life can fall to approximately 4 years before NPV is zero. | |
| 7. | Discount rate | |
| | $3.125 = \text{AF for 5 years } @ x \%$ | |
| | From tables AF for 5 year @ 18% is 3.127, so x is approximately 18% | |
| | i.e. an increase of 80% $\frac{18\% - 10\%}{10\%}$ before NPV is zero. | |

PROBLEM NO: 17**Calculation of NPV through Sensitivity Analysis:**

| Particulars | Amount (Rs.) |
|--|--------------|
| PV of cash inflows (Rs. 60,00,000 × 3.791) | 2,27,46,000 |
| Initial Project Cost | 2,00,00,000 |
| NPV | 27,46,000 |

| Situation | NPV | Changes in NPV |
|---|---|--|
| Base (Present) | Rs. 27,46,000 | |
| If initial project cost is varied adversely by 10% | (Rs. 2,27,46,000 - Rs. 2,20,00,000*) = Rs. 7,46,000 | $\frac{(\text{Rs. } 27,46,000 - \text{Rs. } 7,46,000)}{\text{Rs. } 27,46,000} = (72.83\%)$ |
| If annual cash inflow is varied adversely by 10% | [Rs. 54,00,000 (revised cash flow) ** × 3.791 - (Rs. 2,00,00,000)] = Rs. 4,71,400 | $\frac{(\text{Rs. } 27,46,000 - \text{Rs. } 4,71,400)}{\text{Rs. } 27,46,000} = 82.83\%$ |
| If cost of capital is varied adversely by 10% i.e. it becomes 11% | (Rs. 60,00,000 × 3.696) - Rs. 2,00,00,000 = Rs. 21,76,000 | $\frac{(\text{Rs. } 27,46,000 - \text{Rs. } 21,76,000)}{\text{Rs. } 27,46,000} = 20.76\%$ |

*Revised initial project Cost = $2,00,00,000 \times 110\% = 2,20,00,000$

**Revised Cash Flow = $\text{Rs. } 60,00,000 \times (100 - 10)\% = \text{Rs. } 54,00,000$

Conclusion: Project is most sensitive to 'annual cash inflow'.

PROBLEM NO: 18**P.V. of Cash Flows:**

| | | | |
|--------|-----------------------------------|--------------------|-------------------|
| Year 1 | Running Cost | Rs. 4,000 x 0.917 | =(Rs. 3,668) |
| | Savings | Rs. 12,000 x 0.917 | =(Rs. 11,004) |
| Year 2 | Running Cost | Rs. 5,000 x 0.842 | =(Rs. 4,210) |
| | Savings | Rs. 14,000 x 0.842 | =(Rs. 11,788) |
| | | | Rs. 14,914 |
| Year 0 | Less: P.V. of Cash Outflow | Rs.10,000 x 1 | =(Rs. 10,000) |
| | | NPV | Rs. 4,914 |

Sensitivity Analysis:

i) Increase of Plant Value by Rs. 4,914

$$\frac{4,914}{10000} \times 100 = 49.14\%$$

ii) Increase of Running Cost by Rs. 4,914

$$\frac{4,914}{3,668 + 4,210} = \frac{4,914}{7,878} \times 100 = 62.38\%$$

iii) Fall in Saving by Rs. 4,914

$$\frac{4,914}{11,004 + 11,788} = \frac{4,914}{22,792} \times 100 = 21.56\%$$

Hence, savings factor is the most sensitive to affect the acceptability of the project as in Comparison of other two factors as a slight % change in this factor shall more affect the NPV than others

Alternative Solution:

| | | | |
|--------|-----------------------------------|--------------------|-------------------|
| Year 1 | Running Cost | Rs. 4,000 x 0.917 | =(Rs 3,668) |
| | Savings | Rs. 12,000 x 0.917 | =(Rs. 11,004) |
| Year 2 | Running Cost | Rs. 5,000 x 0.842 | =(Rs. 4,210) |
| | Savings | Rs. 14,000 x 0.842 | =(Rs. 11,788) |
| | | | Rs. 14,914 |
| Year 0 | Less: P.V. of Cash Outflow | Rs.10,000 x 1 | =(Rs. 10,000) |
| | | NPV | Rs. 4,914 |

Analysis:**Sensitivity:**

i) If the initial project cost is varied adversely by say 10%*.

$$\text{NPV (Revised)} (\text{Rs.}4,914 - \text{Rs.}1,000) = \text{Rs.}3,914$$

$$\text{Change in NPV} \frac{\text{Rs.}4,914 - \text{Rs.}3,914}{\text{Rs.}4,914} = 20.35\%$$

ii) If annual Running cost is varied by say 10%*.

$$\text{NPV (Revised)} (\text{Rs.}4,914 - \text{Rs.}400 \times 0.917 - \text{Rs.}500 \times 0.843)$$

$$= \text{Rs.}4,914 - \text{Rs.}367 - \text{Rs.}421 = \text{Rs.}4,126$$

$$\text{Change in NPV} \frac{\text{Rs.}4,914 - \text{Rs.}4,126}{\text{Rs.}4,914} = 16.04\%$$

iii) If saving is varied by say 10%.

$$\text{NPV (Revised)} (\text{Rs.}4,914 - \text{Rs.}1,200 \times 0.917 - \text{Rs.}1,400 \times 0.843)$$

$$= \text{Rs.}4,914 - \text{Rs.}1,100 - \text{Rs.}1,180 = \text{Rs.}2,634$$

$$\text{Change in NPV} \frac{\text{Rs.}4,914 - \text{Rs.}2,634}{\text{Rs.}4,914} = 46.40\%$$

Hence, savings factor is the most sensitive to affect the acceptability the project.

- Any % of variation other than 10% can also be assumed.

PROBLEM NO: 19

i) **Step - 1:**

The expected cash flows of the project are as follows:

| Year | $P_r = 0.2$ (Rs.) | $P_r = 0.6$ (Rs.) | $P_r = 0.2$ (Rs.) | Total (Rs.) | PVF | Cash flow (Rs.) |
|---|-------------------|-------------------|-------------------|-------------|--------|-----------------|
| 0 | (1,00,000) | (3,00,000) | (1,00,000) | (5,00,000) | 1 | (5,00,000) |
| 1 | 30,000 | 1,20,000 | 50,000 | 2,00,000 | 0.8 | 1,60,000 |
| 2 | 30,000 | 1,20,000 | 50,000 | 2,00,000 | 0.64 | 1,28,000 |
| 3 | 30,000 | 1,20,000 | 50,000 | 2,00,000 | 0.512 | 1,02,400 |
| 4 | 30,000 | 1,20,000 | 50,000 | 2,00,000 | 0.4096 | 81,920 |
| 4 | 10,000 | 60,000 | 30,000 | 1,00,000 | 0.4096 | 40,960 |
| NPV based on expected cash flows would be as follows | | | | | | 13,280 |

Alternatively:

$$\begin{aligned}
 \text{NPV} &= 2,00,000 \times (\text{PVAF}) + \text{PV of terminal cash flow} - \text{PV of cash out flow} \\
 &= 2,00,000 \times (25\%, 4 \text{ yrs.}) + (1,00,000 \times 0.4096) - 5,00,000 \\
 &= 4,72,320 + 40,960 - 5,00,000 \\
 &= 5,13,280 - 5,00,000 \\
 &= 13,280
 \end{aligned}$$

ii) For the worst case, the cash flows from the cash flow column farthest on the left are used to calculate NPV

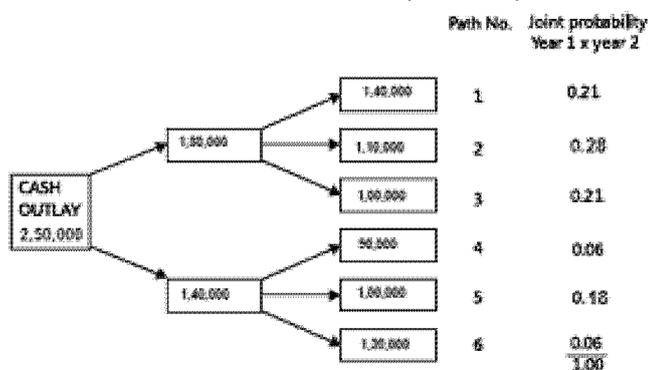
$$\begin{aligned}
 &= -\text{Rs. } 5,00,000 + \frac{\text{Rs. } 1,50,000}{(1+0.25)^1} + \frac{\text{Rs. } 1,50,000}{(1+0.25)^2} + \frac{\text{Rs. } 1,50,000}{(1+0.25)^3} + \frac{\text{Rs. } 1,50,000}{(1+0.25)^4} + \frac{\text{Rs. } 50,000}{(1+0.25)^4} \\
 &= -\text{Rs. } 5,00,000 + \text{Rs. } 1,20,000 + \text{Rs. } 96,000 + \text{Rs. } 76,800 + \text{Rs. } 61,440 + \text{Rs. } 20,480 \\
 \text{NPV} &= -\text{Rs. } 1,25,280
 \end{aligned}$$

For the best case, the cash flows from the cash flow column farthest on the right are used to calculate NPV.

$$\begin{aligned}
 &= -\text{Rs. } 5,00,000 + \frac{\text{Rs. } 2,50,000}{(1+0.25)^1} + \frac{\text{Rs. } 2,50,000}{(1+0.25)^2} + \frac{\text{Rs. } 2,50,000}{(1+0.25)^3} + \frac{\text{Rs. } 2,50,000}{(1+0.25)^4} + \frac{\text{Rs. } 1,50,000}{(1+0.25)^4} \\
 &= -\text{Rs. } 5,00,000 + \text{Rs. } 2,00,000 + \text{Rs. } 1,60,000 + \text{Rs. } 1,28,000 + \text{Rs. } 1,02,400 + \text{Rs. } 61,440 \\
 \text{NPV} &= \text{Rs. } 1,51,840
 \end{aligned}$$

PROBLEM NO: 20

i) The decision tree diagram is presented in the chart, identifying various paths and outcomes, and the computation of various paths/outcomes and NPV of each path are presented in the following tables:



The Net Present Value (NPV) of each path at 15% discount rate is given below:

| Path | Year 1 Cash Flows (Rs.) | Year 2 Cash Flows (Rs.) | Total Cash Inflows (PV) (Rs.) | Cash Outflows (Rs.) | NPV (Rs.) |
|------|-----------------------------------|------------------------------------|-------------------------------|---------------------|-----------|
| 1 | $1,80,000 \times 0.87 = 1,56,600$ | $1,40,000 \times 0.756 = 1,05,840$ | 2,62,440 | 2,50,000 | 12,440 |
| 2 | 1,56,600 | $1,10,000 \times 0.756 = 83,160$ | 2,39,760 | 2,50,000 | (10,240) |
| 3 | 1,56,600 | $1,00,000 \times 0.756 = 75,600$ | 2,32,200 | 2,50,000 | (17,800) |
| 4 | $1,40,000 \times 0.87 = 1,21,800$ | $90,000 \times 0.756 = 68,040$ | 1,89,840 | 2,50,000 | (60,160) |
| 5 | 1,21,800 | $1,00,000 \times 0.756 = 75,600$ | 1,97,400 | 2,50,000 | (52,600) |
| 6 | 1,21,800 | $1,20,000 \times 0.756 = 90,720$ | 2,12,520 | 2,50,000 | (37,480) |

Statement showing Expected Net Present Value

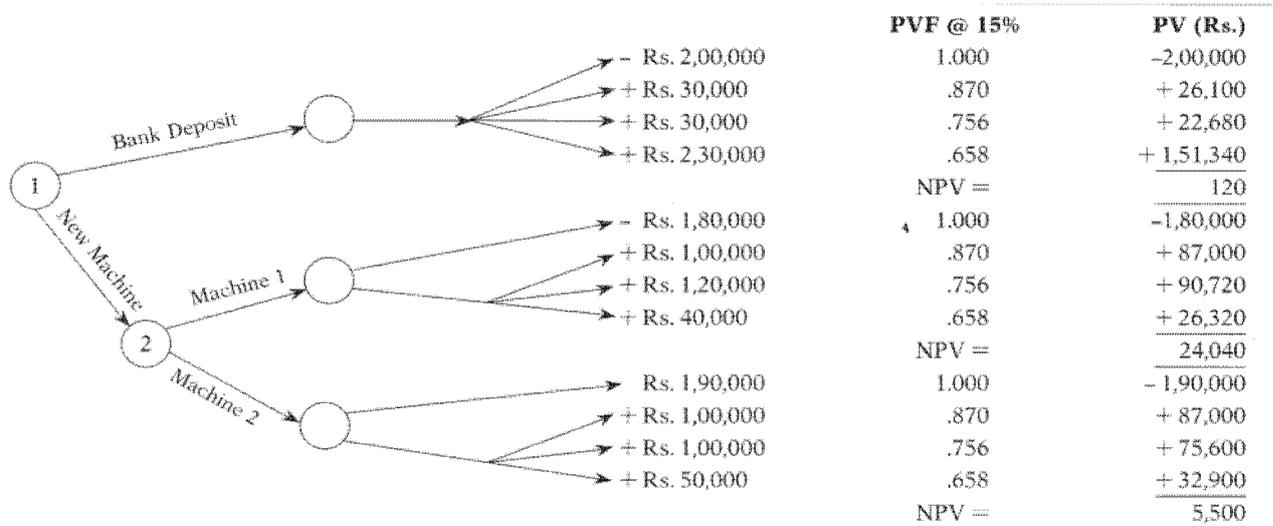
| S.No | NPV (Rs.) | Joint Probability | Expected NPV (Rs.) |
|------|-----------|-------------------|---------------------|
| 1 | 12,440 | 0.21 | 2,612.4 |
| 2 | (10,240) | 0.28 | (2,867.20) |
| 3 | (17,800) | 0.21 | (3,738) |
| 4 | (60,160) | 0.06 | (3,609.6) |
| 5 | (52,600) | 0.18 | (9,468) |
| 6 | (37,480) | 0.06 | (2,248.8) |
| | | | (19,319.2) = 19,319 |

- ii) If the worst outcome is realized the project will yield NPV of Rs. (60,160). The probability of occurrence of this NPV is 6% (Path 4).
- iii) The best outcome will be path 1 when the NPV is at Rs. 12,440. The probability of occurrence of this NPV is 21%.
- iv) The project should be rejected because the Expected NPV is Negative at Rs. 19,319.

Note: Students are advised to rectify the hint answer given in our material.

PROBLEM NO: 21

The above situation can be presented in the form of a decision tree as given in Figure:



On the basis of above Figure, it may be mentioned that the present situation is a two stage decision process. At stage 1, the firm has to decide whether to keep money in liquid form by depositing in a bank @ 12% or to buy a machine for the production of the new product. If the firm selects not to deposit the money in the bank, then to select, in the second stage whether to buy machine 1 or machine 2. It may be noted that if at stage 1, the firm decides to go for bank deposit, then evaluation of machine 1 and machine 2 is not required at all.

PROBLEM NO: 22

Assignment of Random Number.

| Sales (Units) | Prob. | Cumulative Prob. | Random Number assigned. |
|---------------|-------|------------------|-------------------------|
| 2700 | 0.10 | 0.10 | 00 – 09 |
| 2800 | 0.15 | 0.25 | 10- 24 |
| 2900 | 0.20 | 0.45 | 25 – 44 |
| 3000 | 0.35 | 0.80 | 45 – 79 |
| 3100 | 0.15 | 0.95 | 80 – 94 |
| 3200 | 0.05 | 1.00 | 95 - 99 |

Statement Showing Profit/Loss position on Producing 3000 items and 2900 items per day.

| Day | Random Number | Estimated Sales | Profit/Loss today when production = 3000 per day | Profit/Loss today when production = 2900 per day |
|-----|---------------|-----------------|--|--|
| 1 | 11 | 2800 | 2800 × 1-200 ×1.50 = 2500 | 2800 × 1-100 ×1.50 = 2650 |
| 2 | 98 | 3200 | 3000 × 1-200 ×0.50 = 2900 | 2800 × 1-100 ×1.50 = 2650 |
| 3 | 66 | 3000 | 3000 × 1= 3000 | 2900 × 1- 100 ×0.50 = 2850 |
| 4 | 97 | 3200 | 3000 × 1-200 ×0.50 = 2900 | 2900 × 1- 300 ×0.50 = 2750 |

| | | | | |
|----|----|------|--|--|
| 5 | 95 | 3200 | $3000 \times 1-200 \times 0.50 = 2900$ | $2900 \times 1-300 \times 0.50 = 2750$ |
| 6 | 01 | 2700 | $2700 \times 1-300 \times 1.50 = 2250$ | $2700 \times 1-200 \times 1.50 = 2400$ |
| 7 | 79 | 3000 | $3000 \times 10 = 3000$ | $2900 \times 1-100 \times 0.50 = 2850$ |
| 8 | 12 | 2800 | $2800 \times 1-200 \times 1.50 = 2500$ | $2800 \times 1-100 \times 1.50 = 2650$ |
| 9 | 17 | 2800 | $2800 \times 1-200 \times 1.50 = 2500$ | $2800 \times 1-100 \times 1.50 = 2650$ |
| 10 | 21 | 2800 | $2800 \times 1-200 \times 1.50 = 2500$ | $2800 \times 1-100 \times 1.50 = 2650$ |
| | | | 26,950 | 26,950 |

The total profit for next 10 days will be Rs. 26,950, if company manufactures 3000 items per day. In case company decides to produce 2900 items per day profit shall remain unchanged.

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THE END

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